

# Package: hhh4addon (via r-universe)

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**Type** Package

**Title** Extensions to endemic-epidemic timeseries modeling from package surveillance

**Version** 0.0.0.9014

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(substantial parts of the package consist of modified code from  
the surveillance package), R Core Team [ctb] (a few code  
segments are modified versions of code from base R)

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**Description** Extending surveillance::hhh4 to allow for distributed  
lags, solutions for longterm prediction and (periodically)  
stationary moments.

**License** GPL-2

**Encoding** UTF-8

**LazyData** true

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**Imports** fanplot, MASS, nlme, numDeriv

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**Suggests** knitr, rmarkdown

**VignetteBuilder** knitr

**URL** <https://github.com/jbracher/hhh4addon>

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aggregate_moments	<i>Aggregation of stationary or predictive moments</i>
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**Description**

Aggregation of stationary or predictive moments as calculated using `stationary_moments` or `predictive_moments`.

**Usage**

```
aggregate_moments(momentsObj, aggregation_matrix, by_timepoint = FALSE)
```

**Arguments**

- |                                 |                                                                                                                                                                                                                                                                                                                                                                        |
|---------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <code>momentsObj</code>         | an object of class <code>moments_hhh4</code> containing stationary or predictive moments, as returned by <code>stationary_moments</code> or <code>predictive_moments</code>                                                                                                                                                                                            |
| <code>aggregation_matrix</code> | an aggregation matrix with either <code>momentsObj\$n_units</code> columns (for aggregation across units while keeping the temporal structure; set option <code>by_timepoint = TRUE</code> in this case) or <code>length(momentsObj\$mu_vector)</code> (for aggregation that does not preserve the temporal structure; set option <code>by_timepoint = FALSE</code> ). |
| <code>by_timepoint</code>       | logical: is aggregation only across units while preserving the temporal structure? Note that the new <code>moments_hhh4</code> object cannot have the <code>condition</code> , <code>mu_matrix</code> , <code>var_matrix</code> and <code>cov_array</code> elements if the temporal structure is given up.                                                             |

**Value**

An object of class `moments_hhh4` representing the new prediction.

**Examples**

```
# load data:
data("noroBL")

#####
# fit a bivariate model:
controlBL <- list(end = list(f = addSeason2formula(~ -1 + fe(1, unitSpecific = TRUE))),
                  ar = list(f = ~ -1 + fe(1, unitSpecific = TRUE)),
                  ne = list(f = ~ -1 + fe(1, unitSpecific = TRUE)),
                  family = "NegBinM", subset = 2:260) # not a very parsimonious parametrization, but feasible
fitBL <- hhh4(noroBL, control = controlBL)
pred_mom <- predictive_moments(fitBL, t_condition = 260, lgt = 52, return_Sigma = TRUE)
# Sigma is required in order to aggregate predictions.

#####
# plot predictions for two regions:
par(mfrow = 1:2)
```

```

fanplot_prediction(pred_mom, unit = 1, main = "Bremen")
fanplot_prediction(pred_mom, unit = 2, main = "Lower Saxony")

#####
# aggregation 1: combine the two regions
aggr_matr_pool <- matrix(1, ncol = 2)
# specify by_timepoint = TRUE to keep the temporal structure and aggregate only
# counts from the same week:
pred_mom_pooled <- aggregate_moments(pred_mom, aggr_matr_pool, by_timepoint = TRUE)
fanplot_prediction(pred_mom_pooled, unit = 1, ylim = c(0, 500), main = "Aggregation over regions")

#####
# aggregation 2: total burden in the two regions
aggr_matr_total_burden <- matrix(rep(c(1, 0, 0, 1), 52), nrow = 2,
                                    dimnames = list(c("Bremen", "Lower Saxony"),
                                                    NULL))
pred_mom_total_burden <- aggregate_moments(pred_mom, aggr_matr_total_burden)
plot_moments_by_unit(pred_mom_total_burden, main = "Total burdens")

#####
# works also with stationary moments:
stat_mom <- stationary_moments(fitBL, return_Sigma = TRUE)
stat_mom_pooled <- aggregate_moments(stat_mom, aggr_matr_pool, by_timepoint = TRUE)
stat_mom_total_burden <- aggregate_moments(stat_mom, aggr_matr_total_burden, by_timepoint = FALSE)
fanplot_stationary(stat_mom_pooled)
plot_moments_by_unit(stat_mom_total_burden, main = "Total burdens")

```

**ar2\_lag**

*Function to obtain AR2 weights This function generates AR2 weights which are subsequently used inside of get\_weighted\_lags. To be passed to hhh4\_lag or profile\_par\_lag as the control\$funct\_lag argument.*

**Description**

Function to obtain AR2 weights This function generates AR2 weights which are subsequently used inside of get\_weighted\_lags. To be passed to hhh4\_lag or profile\_par\_lag as the control\$funct\_lag argument.

**Usage**

```
ar2_lag(par_lag, min_lag, max_lag)
```

**Arguments**

par_lag	a parameter to steer the lag structure, here $\text{logit}(p)$ where $p$ is the weight of the first lag; see details of hhh4lag or profile_par_lag.
---------	-----------------------------------------------------------------------------------------------------------------------------------------------------

<code>min_lag</code>	smallest lag to include; the support of the Poisson form starts only at <code>min_lag</code> . Defaults to 1.
<code>max_lag</code>	highest lag to include; higher lags are cut off and the remaining weights standardized. Defaults to 5.

`confint.oneStepAhead` *confidence intervals for one-step-ahead predictions*

### Description

confidence intervals for one-step-ahead predictions

### Usage

```
## S3 method for class 'oneStepAhead'
confint(object, parm, level = 0.95, ...)
```

`decompose.hhh4` *A wrapper around* `decompose.hhh4lag` *and* `surveillance::decompose.hhh4`

### Description

A wrapper around `decompose.hhh4lag` and `surveillance::decompose.hhh4` to handle ordinary `hhh4` objects and objects of the new `hhh4lag` class.

### Usage

```
decompose.hhh4(x, coefs = x$coefficients, ...)
```

`decompose.hhh4lag` *A modified version of* `decompose.hhh4`

### Description

A modified version of `decompose.hhh4` to deal with the added features of the `hhh4lag` class.

### Usage

```
## S3 method for class 'hhh4lag'
decompose(x, coefs = x$coefficients, ...)
```

dengueSJ

*Data set on dengue in San Juan, Puerto Rico***Description**

Case counts of dengue in San Juan, Puerto Rico, 1990-2013; stored as an sts object

**Author(s)**

Johannes Bracher

**Source**

Counts retrieved from the supplement of Ray et al (2017): Infectious disease prediction with kernel conditional density estimation, Statistics in Medicine 36(30):4908-4929. These data originally stem from a forecasting competition organized by the US federal government: <http://dengueforecasting.noaa.gov/>

distr\_lag

*Display the function and parameters used for distributed lags***Description**

Display the function and parameters used for distributed lags

**Usage**

```
distr_lag(hhh4obj)
```

**Arguments**

hhh4obj            an object of class hhh4

**Value**

A list containing the function and parameters characterizing the lag weights (for both the ar and ne components)

**Examples**

```
data("salmonella.agona")
## convert old "disProg" to new "sts" data class
salmonella <- disProg2sts(salmonella.agona)
# specify and fit model: fixed geometric lag structure
# with weight 0.8 for first lag
control_salmonella <- list(end = list(f = addSeason2formula(~ 1)),
                           ar = list(f = addSeason2formula(~ 1),
                                     par_lag = 0.8),
```

```
family = "NegBinM", subset = 6:312)
fit_salmonella <- hhh4_lag(salmonella, control_salmonella)
distr_lag(fit_salmonella)
```

**ds\_score\_hhh4***Calculate Dawid-Sebastiani score***Description**

Calculate Dawid-Sebastiani score for a prediction returned by `predictive_moments`.

**Usage**

```
ds_score_hhh4(pred, detailed = FALSE, scaled = TRUE)
```

**Arguments**

<code>pred</code>	the prediction as returned by <code>longterm_prediction_hhh4</code> (and potentially aggregated using <code>aggregate_prediction</code> )
<code>detailed</code>	detailed or less detailed output?
<code>scaled</code>	if <code>detailed == FALSE</code> : scale DSS with 2d?

**Details**

The Dawid-Sebastiani score is defined as

$$DSS = \log(|\Sigma|) + t(Y_{obs} - \mu)\Sigma^{-1}(Y_{obs} - \mu)$$

where  $\mu$  and  $\Sigma$  are the predictive mean and variance, respectively.  $Y_{obs}$  represents the observation that has materialized.

**Value**

If `detailed == FALSE`: the (potentially scaled) Dawid-Sebastiani score. If `detailed == TRUE`: a vector containing the following elements:

- `dawid_sebastiani` the un-scaled Dawid-Sebastiani score
- `term1` value of the log-determinant entering into the un-scaled Dawid-Sebastiani score
- `term2` value of the quadratic form entering into the un-scaled Dawid-Sebastiani score
- `scaled_dawid_sebastiani` the scaled Dawid-Sebastiani score
- `determinant_sharpness` the determinant sharpness (scaled version of `term1`)

## Examples

```
## a simple univariate example:
data("salmonella.agona")
## convert old "disProg" to new "sts" data class
salmonella <- disProg2sts(salmonella.agona)
# specify and fit model: fixed geometric lag structure
# with weight 0.8 for first lag
control_salmonella <- list(end = list(f = addSeason2formula(~ 1)),
                           ar = list(f = addSeason2formula(~ 1),
                                      par_lag = 0.8, use_distr_lag = TRUE),
                           family = "NegBinM", subset = 6:312)
fit_salmonella <- hhh4_lag(salmonella, control_salmonella)
pred_salmonella <- predictive_moments(fit_salmonella, t_condition = 260,
                                         52, return_Sigma = TRUE)
ds_score_hhh4(pred_salmonella, detailed = TRUE)
```

**fanplot\_prediction**      *Display prediction as a fan plot*

## Description

Plots a fanplot to display quantiles of (negative binomial approximations) of the week-wise predictive distributions

## Usage

```
fanplot_prediction(
  pred,
  unit = 1,
  probs = 1:99/100,
  interpolate_probs = TRUE,
  add_observed = TRUE,
  add_pred_means = TRUE,
  fan.col = colorRampPalette(c("darkgreen", "gray90")),
  pt.col = "red",
  pt.cex = 0.6,
  l.col = "black",
  mean.col = "black",
  mean.lty = "dashed",
  ln = NULL,
  rlab = NULL,
  add = FALSE,
  add.legend = FALSE,
  width.legend = 0.1 * (max(pred$timepoints) - min(pred$timepoints))/pred$freq,
  probs.legend = c(1, 25, 50, 75, 99)/100,
  ylim = NULL,
  xlab = "t",
```

```

ylab = "No. infected",
return_matrix = FALSE,
...
)

```

### Arguments

pred	the prediction as returned by longterm_prediction_hhh4 (and potentially aggregated using aggregate_prediction)
unit	numeric denoting the unit to display
probs	vector of probabilities: which quantiles shall be displayed in the fan plot?
interpolate_probs	logical: smooth curves by simple interpolation of quantiles
add_observed	logical: shall observed values be added?
fan.col, ln, rlab	graphical parameters passed on to fanplot::fan
pt.col, pt.cex, l.col	graphical parameters for display of observed values
add	logical: add to existing plot?
add_legend	logical: shall a color key legend be added?
width_legend	width of box for color key legend in user coordinates
probs_legend	vector of probabilities to display in the legend
ylim	limit for the y-axis, passed to plot()
xlab, ylab	axis labels
return_matrix	logical: return matrix passed to fanplot::fan; useful to make more sophisticated plots.
...	other arguments passed on to plot()

### Value

Only if return\_matrix set to TRUE: the matrix passed to fanplot::fan

### Examples

```

data("salmonella.agona")
# convert old "disProg" to new "sts" data class:
salmonella <- disProg2sts(salmonella.agona)
control_salmonella <- list(end = list(f = addSeason2formula(~ 1), lag = 1),
                           ar = list(f = addSeason2formula(~ 1), lag = 1),
                           family = "NegBinM", subset = 6:250)
fit_salmonella <- hhh4_lag(salmonella, control_salmonella) # fit model
# obtain prediction:
pred_mom <- predictive_moments(fit_salmonella, t_condition = 250, lgt = 52)
# plot the prediction only:
fanplot_prediction(pred_mom, add_legend = TRUE)
# or plot it along with the fit:

```

```
plot(fit_salmonella)
fanplot_prediction(pred_mom, add = TRUE) # add fan plot
```

**fanplot\_stationary**      *Display stationary distribution as a fanplot*

## Description

Plots a fanplot to display quantiles of (negative binomial approximations) of the week-wise stationary distributions

## Usage

```
fanplot_stationary(
  stat_mom,
  unit = 1,
  probs = 1:99/100,
  interpolate_probs = TRUE,
  add_pred_means = TRUE,
  fan.col = colorRampPalette(c("darkgreen", "gray90")),
  pt.col = "red",
  pt.cex = 0.3,
  l.col = "black",
  mean.col = "black",
  mean.lty = "dashed",
  ln = NULL,
  ln.col = "red",
  rlab = NULL,
  style = "fan",
  add = FALSE,
  timepoints = 1:nrow(stat_mom$mu_matrix)/stat_mom$freq,
  add_legend = FALSE,
  width.legend = 0.1 * (max(timepoints) - min(timepoints)),
  probs.legend = c(1, 25, 50, 75, 99)/100,
  hlines = NULL,
  vlines = NULL,
  ylim = NULL,
  xlab = "t",
  ylab = "No. infected",
  return_matrix = FALSE,
  ...
)
```

## Arguments

<code>stat_mom</code>	the stationary moments as returned by <code>stationary_moments_hhh4</code> (and potentially aggregated using <code>aggregate_prediction</code> )
-----------------------	--------------------------------------------------------------------------------------------------------------------------------------------------

unit	numeric denoting the unit to display
probs	vector of probabilities: which quantiles shall be displayed in the fan plot?
interpolate_probs	logical: smooth curves by simple interpolation of quantiles
add_pred_means	logical: add line showing the predictive means
fan.col, ln, ln.col, rlab, style	graphical parameters passed on to fanplot::fan
pt.col, pt.cex, l.col	graphical parameters for display of observed values
add	logical: add to existing plot?
timepoints	vector giving the x-coordinates for the fanplot (generates start and frequency for fanplot::fan)
add_legend	logical: shall a color key legend be added?
width_legend	width of box for color key legend in user coordinates
probs_legend	vector of probabilities to display in the legend
hlines, vlines	coordinates for horizontal and vertical grid lines
ylim	limit for the y-axis, passed to plot()
xlab, ylab	axis labels
return_matrix	logical: return matrix passed to fanplot::fan; useful to make more sophisticated plots.
...	other arguments passed on to plot()
means_col, mean_lty	graphical parameters for display of predictive means

## Value

Only if `return_matrix` set to TRUE: the matrix passed to `fanplot::fan`

## Examples

```

data("salmonella.agona")
## convert old "disProg" to new "sts" data class
salmonella <- disProg2sts(salmonella.agona)
# specify and fit model
control_salmonella <- list(end = list(f = addSeason2formula(~ 1), lag = 1),
                           ar = list(f = addSeason2formula(~ 1), lag = 1),
                           family = "NegBinM")
fit_salmonella <- hhh4(salmonella, control_salmonella)
# obtain periodically stationary moments:
stat_mom <- stationary_moments(fit_salmonella)
# plot periodically stationary means:
fanplot_stationary(stat_mom, add_legend = TRUE)
# add paths of the six seasons in the data set:
for(i in 0:5{
  lines(1:52/52, salmonella@observed[(i*52 + 1):(i + 1)*52]], col = "blue")
}
legend("topleft", col = "blue", lty = 1, legend = "observed seasons")

```

---

**fit\_par\_lag***Estimating the lag decay parameter of an hhh4\_lag model using profile likelihood*

---

## Description

Wrapper around `hhh4_lag` to allow for profile likelihood estimation of the scalar parameter governing the lag structure. `hhh4_lag` can fit models with fixed lag decay parameter; `fit_par_lag` loops around it and tries a set of possible parameters provided in the argument `range_par`. NOTE: this will soon be replaced by `profile_par_lag` which does the same, but using `optim...`, `method = "Brent"`, ...).

## Usage

```
fit_par_lag(
  stsObj,
  control,
  check.analyticals = FALSE,
  range_par,
  use_update = TRUE
)
```

## Arguments

- |                         |                                                                                                                          |
|-------------------------|--------------------------------------------------------------------------------------------------------------------------|
| <code>range_par</code>  | a vector of values to try for the <code>par_lag</code> argument of <code>funct_lag</code>                                |
| <code>use_update</code> | should results from previous values in <code>range_par</code> be used as starting value for next iteration (via update)? |

## Details

In this modified version of `surveillance::hhh4`, distributed lags can be specified by additional elements `control` argument:

- `funct_lag` Function to compute the lag weights  $u_q$  (see details) depending on a scalar parameter `par_lag`. The function has to take the following arguments:
  - `par_lag` A scalar parameter to steer  $u_q$ . It should be specified in a way which allows it to take any value in the real numbers
  - `min_lag`, `max_lag` Minimum and maximum lags; e.g. `min_lag = 3`, `max_lag = 6` will assign all weights to lags 3 through 6. Usually `min_lag` is set to 1, higher values can be useful for direct forecasting at higher horizons. `max_lag` defaults to 5, which is often reasonable for weekly data, but should likely be increased when using daily data.
- `min_lag`, `max_lag` Specification of the arguments passed to `funct_lag` to compute the distributed lags. Unlike in `hhh4_lag`, `par_lag` is not to be specified as it is estimated from the data. Important: the first element of the `subset` argument in `control` needs to be larger than `max_lag` (as for the first `max_lag` observations the fitted values cannot be computed)

Unlike in `hhh4_lag` the `par_lag` argument for `funct_lag` is not specified directly by the user; instead the model is re-fit for each parameter value provided in `range_par`.

#` @paramstsObj,control,check.analyticals As in `surveillance::hhh4`, but `control` allows for some additional elements in order to specify a distributed lag structure:

- `funct_lag` Function to compute the lag weights  $u_q$  (see details) depending on a scalar parameter `par_lag`. The function has to take the following arguments:
  - `par_lag` A scalar parameter to steer  $u_q$ . It should be specified in a way which allows it to take any value in the real numbers
  - `min_lag, max_lag` Minimum and maximum lags; e.g. `min_lag = 3, max_lag = 6` will assign all weights to lags 3 through 6. Usually `min_lag` is set to 1, higher values can be useful for direct forecasting at higher horizons.
- `min_lag, max_lag` Specification of the arguments passed to `funct_lag` to compute the distributed lags. Unlike in `hhh4_lag`, `par_lag` is not to be specified as it is estimated from the data.

## Value

A list including the best model among all fitted ones (`best_mod`) and a vector of the AIC values obtained for the different values provided in `range_par` (AICs)

## See Also

`hhh4_lag` for fitting models with fixed `par_lag`; `profile_par_lag` for optimization using `optim` rather than a vector `range_par` of potential values.

## Examples

```
## a simple univariate example:
data("salmonella.agona")
## convert old "disProg" to new "sts" data class
salmonella <- disProg2sts(salmonella.agona)
# specify and fit model: fixed geometric lag structure
control_salmonella <- list(end = list(f = addSeason2formula(~ 1)),
                           ar = list(f = addSeason2formula(~ 1)),
                           family = "NegBinM", subset = 6:312)
# get a reasonable range of values for par_lag. par_lag is logit(p) in teh
# geometric lag function
grid_p <- seq(from = 0.01, to = 0.99, by = 0.02)
grid_par_lag <- log(grid_p/(1 - grid_p))
fit_salmonella <- fit_par_lag(salmonella, control_salmonella, range_par = grid_par_lag)
summary(fit_salmonella$best_mod)
plot(fit_salmonella$AICs, xlab = "p", ylab = "AIC")
# 0.56 on first lag
#
# re-fit with Poisson lags:
control_salmonella2 <- control_salmonella
control_salmonella2$funct_lag = poisson_lag
grid_p2 <- seq(from = 0.01, to = 2, by = 0.02)
grid_par_lag2 <- log(grid_p2)
```

```
fit_salmonella2 <- fit_par_lag(salmonella, control_salmonella2, range_par = grid_par_lag2)
summary(fit_salmonella2$best_mod)
# leads to somewhat different decay and very slightly better AIC
```

**fixef.hhh4lag***A modified version of fixef.hhh4***Description**

A modified version of fixef.hhh4

**Usage**

```
## S3 method for class 'hhh4lag'
fixef(object, ...)
```

**geometric\_lag**

*Function to obtain geometric weights This function generates geometric weights which are subsequently used inside of get\_weighted\_lags. To be passed to hhh4\_lag or profile\_par\_lag as the control\$funct\_lag argument.*

**Description**

Function to obtain geometric weights This function generates geometric weights which are subsequently used inside of get\_weighted\_lags. To be passed to hhh4\_lag or profile\_par\_lag as the control\$funct\_lag argument.

**Usage**

```
geometric_lag(par_lag, min_lag, max_lag)
```

**Arguments**

- |                |                                                                                                                                                                                                      |
|----------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>par_lag</b> | a parameter to steer the lag structure, here $\text{logit}(p)$ where $p$ is the parameter of the geometric distribution characterizing the lag structure; see details of hhh4lag or profile_par_lag. |
| <b>min_lag</b> | smallest lag to include; the support of the Poisson form starts only at min_lag. Defaults to 1.                                                                                                      |
| <b>max_lag</b> | highest lag to include; higher lags are cut off and the remaining weights standardized. Defaults to 5.                                                                                               |

---

get\_diags\_of\_array      *Get diagonal elements of all slices of an array*

---

## Description

Extracts diagonals of all slices of an array (i.e. of `arr[, , 1]`, `arr[, , 2]`, ... and stacks them in one vector.)

## Usage

```
get_diags_of_array(arr)
```

## Arguments

`arr`                  An array.

---

get\_weighted\_lags      *Transform matrix of first-order lagged observations to matrix of weighted sums of past observation*

---

## Description

This function modifies the design matrices from first-order lags to weighted lags with weighted structure. Used within `weightedSumNE` and `weightedSumAR`.

## Usage

```
get_weighted_lags(lag1, lag_weights, sum_up = FALSE)
```

## Arguments

`lag1`                  a matrix of first lags as usually used in `hhh4`.

`sum_up`                `sum_up = FALSE` returns a more detailed output; for debugging only.

`lag_weights`           a vector of weights; the length of this vector determines the number of lags.

---

*hhh4\_lag**Fitting hhh4 models with distributed lags*

---

## Description

A modified version of `surveillance::hhh4` to allow for distributed lags. Usually used from inside of the wrappers `profile_par_lag` or `fit_par_lag`.

## Usage

```
hhh4_lag(
  stsObj,
  control = list(ar = list(f = ~-1, offset = 1, lag = NA), ne = list(f = ~-1, offset = 1,
    lag = NA, weights = neighbourhood(stsObj) == 1, scale = NULL, normalize = FALSE), end
    = list(f = ~1, offset = 1), family = c("Poisson", "NegBin1", "NegBinM"), funct_lag =
    geometric_lag, par_lag = 1, min_lag = 1, max_lag = 5, subset = 6:nrow(stsObj),
    optimizer = list(stop = list(tol = 1e-05, niter = 100), regression = list(method =
    "nlminb"), variance = list(method = "nlminb")), verbose = FALSE, start = list(fixed =
    NULL,
    random = NULL, sd.corr = NULL), data = list(t = stsObj@epoch -
    min(stsObj@epoch)), keep.terms = FALSE),
  check.analyticals = FALSE
)
```

## Arguments

`stsObj, control, check.analyticals`

As in `surveillance::hhh4`, but with the following additional elements in the `control` argument in order to specify a distributed lag structure:

- `funct_lag` Function to compute the lag weights  $u_q$  (see details) depending on a scalar parameter `par_lag`. The function has to take the following arguments:
  - `par_lag` A scalar parameter to steer  $u_q$ . It should be specified in a way which allows it to take any value in the real numbers
  - `min_lag, max_lag` Minimum and maximum lags; e.g. `min_lag = 3, max_lag = 6` will assign all weights to lags 3 through 6. Usually `min_lag` is set to 1, higher values can be useful for direct forecasting at higher horizons.
- `par_lag, min_lag, max_lag` Specification of the arguments passed to `funct_lag` to compute the distributed lags. Important: the first element of the `subset` argument in `control` needs to be larger than `max_lag` (as for the first `max_lag` observations the fitted values cannot be computed)

`hhh4_lag` requires `par_lag` to be pre-specified (with a default of 1). Using the wrappers `profile_par_lag` and `fit_par_lag` it can also be estimated using a profile likelihood approach.

## Details

The standard hhh4 function only allows for models with first lags i.e. of the form

$$mu_{it} = \lambda_{it} X_{i,t-1} + \phi_{it} \sum_{j \neq i} w_{ji} X_{j,t-1} + \nu_{it},$$

see ?hhh4. The extension hhh4\_lag allows to specify models of the form

$$mu_{it} = \lambda_{it} \sum_{q=1}^Q u_q X_{i,t-q} + \phi_{it} \sum_{j \neq i} \text{sum}_{q=1}^Q w_{ji} u_q X_{j,t-q} + \nu_{it}.$$

Here the first lags are now replaced by weighted sums of the Q previous observations. The weights  $u_q$ ,  $q = 1, \dots, Q$  sum up to 1 and need to be parametrizable by a single scalar parameter. The value of this parameter needs to be passed as control\$par\_lag. Moreover, a function to obtain a vector of weights from par\_lag needs to be provided in control\$funct\_lag. Currently four such functions are implemented in the package:

- Geometric lags (function geometric\_lag; the default). These are specified as

$$u0_q = \alpha * (1 - \alpha)^{q-1}$$

and  $u_q = u0_q / \text{sum}_{q=1}^Q u0_q$  for  $q = 1, \dots, Q$ . The par\_lag parameter corresponds to  $\text{logit}(\alpha)$ , i.e. the un-normalized weight of the first lag.

- Poisson lags (function poisson\_lag). These are specified as

$$u0_q = \alpha^{(q-1)} \exp(-\alpha) / (q-1)!,$$

and  $u_q = u0_q / \text{sum}_{q=1}^Q u0_q$  for  $q = 1, \dots, Q$ . Note that the Poisson distribution is shifted by one to achieve a positive support. The par\_lag parameter corresponds to  $\log(\alpha)$ .

- Linearly decaying weights (in function linear\_lag). These are specified as

$$u0_q = \max(1 - mq, 0)$$

and  $u_q = u0_q / \text{sum}_{q=1}^Q u0_q$  for  $q = 1, \dots, Q$ . The par\_lag parameter corresponds to  $\text{logit}(m)$ .

- A weighting only between first and second lags (in function ar2lag), i.e.

$$u_1 = \alpha, u_2 = 1 - \alpha.$$

The par\_lag parameter corresponds to  $\text{logit}(\alpha)$ .

Users can specify their own weighting functions as long as they take the arguments described above and return a vector of weights.

## See Also

`profile_par_lag` and `fit_par_lag` estimate par\_lag in a profiling procedure. `profile_par_lag` is the recommended function, `fit_par_lag` may be quicker for complex models.

## Examples

```
## a simple univariate example:
data("salmonella.agona")
## convert old "disProg" to new "sts" data class
salmonella <- disProg2sts(salmonella.agona)
# specify and fit model: fixed geometric lag structure
# with weight 0.8 for first lag
# par_lag is the logit of alpha:
par_lag <- log(0.8/(1 - 0.8))
control_salmonella <- list(end = list(f = addSeason2formula(~ 1)),
                           ar = list(f = addSeason2formula(~ 1)),
                           family = "NegBinM", subset = 6:312,
                           par_lag = par_lag)
fit_salmonella <- hhh4_lag(salmonella, control_salmonella)
summary(fit_salmonella)
# has indeed weight 0.8 on first lag
#
# re-fit with Poisson lags:
par_lag2 <- log(1.2)
control_salmonella2 <- control_salmonella
control_salmonella2$funct_lag = poisson_lag
control_salmonella2$par_lag <- par_lag2
fit_salmonella2 <- hhh4_lag(salmonella, control_salmonella2)
summary(fit_salmonella2)
# the Poisson lag actually allows you to put more weight on
# the second than on the first lag.
```

interpolate\_qnbinom     *Interpolate between quantiles to avoid edgy display*

## Description

An auxiliary function used in fanplot\_prediction, fanplot\_stationary

## Usage

```
interpolate_qnbinom(p, ...)
```

## Arguments

p	A vector of probabilities for which to obtain interpolated quantiles
...	other arguments passed on to pnbinom

---

**is\_complex\_neighbourhood**

*Determine whether an hhh4 object was fitted using one of the more complex techniques for handling neighbourhoods*

---

**Description**

Determine whether an hhh4 object was fitted using one of the more complex techniques for handling neighbourhoods

**Usage**

```
is_complex_neighbourhood(hhh4obj)
```

**Arguments**

hhh4obj            an hhh4 object

---

**is\_fitted\_par\_lag**

*Check if the par\_lag parameter was fitted*

---

**Description**

Check if the par\_lag parameter was fitted

**Usage**

```
is_fitted_par_lag(object)
```

---

**lambda\_tilde**

*Extracting Lambda\_Tilde from an hhh4 object with complex neighbourhood structure*

---

**Description**

A wrapper around lambda\_tilde\_complex\_neighbourhood and lambda\_tilde\_simple\_neighbourhood.

**Usage**

```
lambda_tilde(hhh4obj, subset = NULL, periodic = FALSE)
```

**Arguments**

hhh4obj            a hhh4 object for which to extract Lambda\_tilde  
subset              a subset (in time); only required when periodic == FALSE  
periodic           choose subset to correspond to one full cycle

**lambda\_tilde\_complex\_neighbourhood**

*Extracting Lambda\_Tilde from an hhh4 object with complex neighbourhood structure*

**Description**

Extracting Lambda\_Tilde from an hhh4 object with complex neighbourhood structure. Used for calculations of longterm predictions and stationary distributions.

**Usage**

```
lambda_tilde_complex_neighbourhood(hhh4obj, subset = NULL, periodic = FALSE)
```

**Arguments**

hhh4obj	a hhh4 object for which to extract Lambda_tilde
subset	a subset (in time); only required when periodic == FALSE
periodic	choose subset to correspond to one full cycle

**linear\_lag**

*Function to obtain linearly decaying weights*

**Description**

This function generates linearly decaying weights which are subsequently used inside of `get_weighted_lags`. To be passed to `hhh4_lag` or `profile_par_lag` as the `control$funct_lag` argument. There are different ways of specifying linearly decaying weights, the version implemented here is

$$u0_q = \max(1 - mq, 0)$$

and  $u_q = u0_q / \sum_{q=1}^Q u0_q$  for  $q = 1, \dots, Q$ .

**Usage**

```
linear_lag(par_lag, min_lag, max_lag)
```

**Arguments**

par_lag	a parameter to steer the lag structure, here $\text{logit}(m)$ where $m$ is the linear decay factor; see details of <code>hhh4lag</code> or <code>profile_par_lag</code> .
min_lag	smallest lag to include; the support of the Poisson form starts only at <code>min_lag</code> . Defaults to 1.
max_lag	highest lag to include; higher lags are cut off and the remaining weights standardized. Defaults to 5.

---

`logLik.hhh4lag`*A modified version of logLik.hhh4*

---

### Description

A modified version of `terms.hhh4` to deal with the added features of the `logLik.hhh4` class.

### Usage

```
## S3 method for class 'hhh4lag'
logLik(object, ...)
```

---

`log_normal_lag`

*#' This function generates (shifted) discrete gamma weights which are subsequently used inside of get\_weighted\_lags. To be passed #' to hhh4\_lag or profile\_par\_lag as the control\$funct\_lag argument. #' @param par\_lag a parameter vector of length 2 to steer the lag structure, here log(shape) and log(rate), #' where shape and rate are the parameters of the discrete gamma distribution as implemented in the extraDistr package. #' @param min\_lag smallest lag to include; the support of the Poisson form starts only at min\_lag. Defaults to 1. #' @param max\_lag highest lag to include; higher lags are cut off and the remaining weights standardized. Defaults to 5. #' @author Maria Dunbar, Johannes Bracher #' @export This function generates discretized log-normal weights which are subsequently used inside of get\_weighted\_lags. To be passed to hhh4\_lag or profile\_par\_lag as the control\$funct\_lag argument.*

---

### Description

*#' This function generates (shifted) discrete gamma weights which are subsequently used inside of get\_weighted\_lags. To be passed #' to hhh4\_lag or profile\_par\_lag as the control\$funct\_lag argument. #' @param par\_lag a parameter vector of length 2 to steer the lag structure, here log(shape) and log(rate), #' where shape and rate are the parameters of the discrete gamma distribution as implemented in the extraDistr package. #' @param min\_lag smallest lag to include; the support of the Poisson form starts only at min\_lag. Defaults to 1. #' @param max\_lag highest lag to include; higher lags are cut off and the remaining weights standardized. Defaults to 5. #' @author Maria Dunbar, Johannes Bracher #' @export This function generates discretized log-normal weights which are subsequently used inside of get\_weighted\_lags. To be passed to hhh4\_lag or profile\_par\_lag as the control\$funct\_lag argument.*

### Usage

```
log_normal_lag(par_lag, min_lag, max_lag)
```

**Arguments**

<code>par_lag</code>	a parameter vector of length 2 to steer the lag structure, here $meanlog$ and $log(sdlog)$ , where $meanlog$ and $sdlog$ are the parameters of the log-normal distribution.
<code>min_lag</code>	smallest lag to include; the support of the Poisson form starts only at <code>min_lag</code> . Defaults to 1.
<code>max_lag</code>	highest lag to include; higher lags are cut off and the remaining weights standardized. Defaults to 5.

**Author(s)**

Maria Dunbar, Johannes Bracher

**`matrix_is_cyclic`**      *Check whether the rows of a matrix show a cyclic pattern*

**Description**

Needed to determine whether `stationary_moments` is applicable (works only for models with periodic parameter structure)

**Usage**

```
matrix_is_cyclic(matr, length_of_period)
```

**Arguments**

<code>matr</code>	The parameter matrix to check.
<code>length_of_period</code>	Usually 52 (52 weeks per year).

**Value**

logical: does the matrix show a periodic pattern?

---

neOffsetArray.hhh4lag *A modified version of neOffsetArray*

---

### Description

A modified version of neOffsetArray to deal with the added features of the hhh4lag class.

### Usage

```
neOffsetArray.hhh4lag(  
  object,  
  pars = coefW(object),  
  subset = object$control$subset  
)
```

---

noroBL

*Data set on norovirus gastroenteritis in Bremen and Lower Saxony*

---

### Description

Case counts of norovirus gastroenteritis in the German states of Bremen and Lower Saxony, 2011-2017; stored as an sts object

Case counts of rotavirus gastroenteritis in the German states of Bremen and Lower Saxony, 2011-2017; stored as an sts object

Case counts of campylobacteriosis in the German states of Bremen and Lower Saxony, 2011-2017; stored as an sts object

Case counts of norovirus gastroenteritis in the twelve districts of Berlin, Germany, 2011-2017; stored as an sts object

Case counts of rotavirus gastroenteritis in the twelve districts of Berlin, Germany, 2011-2017; stored as an sts object

### Author(s)

Johannes Bracher

### Source

Surveillance counts retrieved from SurvStat@RKI 2.0 service (<https://survstat.rki.de>), Robert Koch Institute, Berlin as of 30 May 2017.

Surveillance counts retrieved from SurvStat@RKI 2.0 service (<https://survstat.rki.de>), Robert Koch Institute, Berlin as of 30 May 2017.

Surveillance counts retrieved from SurvStat@RKI 2.0 service (<https://survstat.rki.de>), Robert Koch Institute, Berlin as of 30 May 2017.

Surveillance counts retrieved from SurvStat@RKI 2.0 service (<https://survstat.rki.de>), Robert Koch Institute, Berlin.

Surveillance counts retrieved from SurvStat@RKI 2.0 service (<https://survstat.rki.de>), Robert Koch Institute, Berlin.

### **numeric\_fisher\_hhh4lag**

*Numerical evaluation of the covariance matrix including the additional parameter par\_lg*

#### **Description**

Numerical evaluation of the covariance matrix including the additional parameter `par_lg`

#### **Usage**

```
numeric_fisher_hhh4lag(best_mod)
```

#### **Arguments**

<code>best_mod</code>	an <code>hhh4lag</code> object; should be generated in <code>profile_par_lag</code> so that the <code>par_lag</code> parameter is already optimized.
-----------------------	------------------------------------------------------------------------------------------------------------------------------------------------------

### **oneStepAhead\_hhh4lag    *Predictive Model Assessment for hhh4\_lag Models***

#### **Description**

A version of `surveillance::oneStepAhead` for `hhh4_lag` objects. NOTE: by default the `lag_par` parameter is not re-fit in this function!

#### **Usage**

```
oneStepAhead_hhh4lag(
  result,
  tp,
  type = c("rolling", "first", "final"),
  refit_par_lag = FALSE,
  which.start = c("current", "final"),
  keep.estimates = FALSE,
  verbose = TRUE,
  cores = 1
)
```

#### **Arguments**

<code>refit_par_lag</code>	Only new argument compared to <code>surveillance::oneStepAhead</code> : should the lag weighting parameter <code>lag_par</code> be re-fitted in each iteration? Defaults to FALSE.
----------------------------	------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------

`plot.oneStepAhead`      *simple plot of one-step-ahead forecasts*

### Description

simple plot of one-step-ahead forecasts

### Usage

```
## S3 method for class 'oneStepAhead'
plot(x, unit = 1, probs = 1:99/100, start = NULL, means.args = NULL, ...)
```

`plot_moments_by_unit`    *Plot predictive or stationary moments by unit*

### Description

Plot negative binomial approximation of predictive or stationary distributions. Usually to be used with aggregated predictions (where columns correspond to regions or age groups; no temporal structure kept).

### Usage

```
plot_moments_by_unit(
  mom,
  probs = 1:99/100,
  add_observed = TRUE,
  add_pred_means = TRUE,
  fan.col = colorRampPalette(c("darkgreen", "gray90")),
  pt.col = "red",
  pt.cex = 0.3,
  mean_col = "black",
  mean_lty = "dashed",
  ln = NULL,
  rlab = NULL,
  style = "boxfan",
  space = 0.5,
  add_legend = FALSE,
  probs_legend = c(1, 25, 50, 75, 99)/100,
  ylim = NULL,
  main = NULL,
  xlab = NULL,
  las = NULL,
  axes = TRUE,
  ...
)
```

## Arguments

mom	an object of class <code>predictive_moments_hhh4</code> or <code>stationary_moments_hhh4</code> , usually an aggregated prediction without temporal structure (aggregated using <code>aggregate_prediction</code> )
probs	probabilities displayed in fanplot (passed to <code>fanplot::fan</code> )
add_observed	should observed values be added to the plot?
fan.col	color palette for fanplot (passed to <code>fanplot::fan</code> )
pt.col, pt.cex	point color and size for observations
mean_col, mean_lty	line color and type for predictive/stationary means
ln, rlab, style, space	additional arguments passed to <code>fanplot::fan</code> )
add_legend	should a legend with the colour coding be added?
probs_legend	probabilities to be displayed in the legend
ylim, main, xlab, las, axes	usual plotting parameters

## Examples

```
# load data:
data("noroBL")

#####
# fit a bivariate model:
controlBL <- list(end = list(f = addSeason2formula(~ -1 + fe(1, unitSpecific = TRUE))),
                    ar = list(f = ~ -1 + fe(1, unitSpecific = TRUE)),
                    ne = list(f = ~ -1 + fe(1, unitSpecific = TRUE)),
                    family = "NegBinM", subset = 2:260) # not a very parsimonious parametrization, but feasible
fitBL <- hhh4(noroBL, control = controlBL)
pred_mom <- predictive_moments(fitBL, t_condition = 260, lgt = 52, return_Sigma = TRUE)
# Sigma is required in order to aggregate predictions.

#####
# perform an aggregation over time: total burden in the two regions
aggr_matr_total_burden <- matrix(rep(c(1, 0, 0, 1), 52), nrow = 2,
                                     dimnames = list(c("Bremen", "Lower Saxony"),
                                                    NULL))
pred_mom_total_burden <- aggregate_moments(pred_mom, aggr_matr_total_burden)
plot_moments_by_unit(pred_mom_total_burden, main = "Total burden 2016", add_legend = TRUE)
```

`poisson_lag`

*Function to obtain Poisson weights This function generates Poisson weights which are subsequently used inside of `get_weighted_lags`. To be passed to `hhh4_lag` or `profile_par_lag` as the `control$funct_lag` argument.*

### Description

Function to obtain Poisson weights This function generates Poisson weights which are subsequently used inside of get\_weighted\_lags. To be passed to hhh4\_lag or profile\_par\_lag as the control\$funct\_lag argument.

### Usage

```
poisson_lag(par_lag, min_lag, max_lag)
```

### Arguments

par_lag	a parameter to steer the lag structure, here $\log(\mu)$ where $\mu$ is the parameter of the Poisson distribution characterizing the lag structure; see details of hhh4lag or profile_par_lag.
min_lag	smallest lag to include; the support of the Poisson form starts only at min_lag. Defaults to 1.
max_lag	highest lag to include; higher lags are cut off and the remaining weights standardized. Defaults to 5.

**predictive\_moments**      *Analytical computation of predictive moments for an hhh4 model*

### Description

This functions calculates the predictive mean vector and covariance matrix for a path forecast from an hhh4 model.

### Usage

```
predictive_moments(
  hhh4obj,
  t_condition,
  lgt,
  return_Sigma = FALSE,
  return_cov_array = FALSE,
  return_mu_decomposed = FALSE,
  return_M = FALSE
)
```

### Arguments

hhh4obj	an hhh4 object
t_condition	the index of the week on which to condition the path forecast, i.e. an integer between 1 and nrow(hhh4obj\$sts0bj@observed). If you need forecasts beyond the end of your observed time series you need to artificially prolong the sts object used by adding NA values to the end.

<code>lgt</code>	the length of the path forecast, i.e. 52 for forecasting an entire season when using weekly data
<code>return_Sigma</code>	logical: should the entire variance-covariance matrix of the forecast be returned? defaults to FALSE in order to save storage.
<code>return_cov_array</code>	logical: should an array with week-wise covariance matrices be returned?
<code>return_mu_decomposed</code>	logical: should an array with the predictive means decomposed into the different components be returned?
<code>return_M</code>	logical: should the matrix M containing the predictive first and (un-centered) second moments be returned?

### Value

An object of class `predictive_moments_hhh4` containing the following components:

- `mu_matrix` A matrix containing the predictive means. Each row corresponds to a time period and each column to a unit.
- `var_matrix` A matrix containing the predictive variances.
- `cov_array` An array containing time period-wise variance-covariance matrices.
- `mu_vector` as `mu_matrix`, but flattened into a vector.
- `Sigma` a large covariance matrix for all elements of the prediction (corresponding to `mu_vector`)
- `M` a matrix containing predictive means and (un-centered) second moments, specifically  $E(c(1, X))$  shall be forecasted. Important in the internal calculation, accessible mainly for de-bugging purposes.
- `mu_decomposed` an array with the same number of rows and columns as `mu_matrix`, but three layers corresponding to the contributions of the three components to the means
- `start` the index (in the original `sts` object) of the first time period of the prediction
- `freq` the length of a cycle
- `n_units` the number of units covered in the prediction
- `timepoints` the timepoints covered by the prediction etc.
- `timepoints` as `timepoints`, but calendar time rather than indices
- `condition` A matrix containing the realizations for the conditioning time period (or periods)
- `realizations_matrix` A matrix containing the realizations that have materialized in the period covered by the prediction.
- `type` "predictive"; to distinguish from stationary moments.
- `has_temporal_structure` does the object still have the original temporal structure? can be set to FALSE when aggregated using `aggregate_prediction`.

## Examples

```

data("salmonella.agona")
# convert old "disProg" to new "sts" data class:
salmonella <- disProg2sts(salmonella.agona)
control_salmonella <- list(end = list(f = addSeason2formula(~ 1), lag = 1),
                           ar = list(f = addSeason2formula(~ 1), lag = 1),
                           family = "NegBinM", subset = 6:250)
fit_salmonella <- hhh4_lag(salmonella, control_salmonella) # fit model
# obtain prediction:
pred_mom <- predictive_moments(fit_salmonella, t_condition = 250, lgt = 52)
plot(fit_salmonella)
fanplot_prediction(pred_mom, add = TRUE) # add fan plot

```

print.hhh4lag

*A modified version of surveillance::print.hhh4*

## Description

A modified version of surveillance::print.hhh4 to deal with the added features of the hhh4lag class.

## Usage

```

## S3 method for class 'hhh4lag'
print(x, digits = max(3,getOption("digits") - 3), ...)

```

print.summary.hhh4lag *A modified version of print.summary.hhh4*

## Description

A modified version of print.summary.hhh4 to deal with the added features of the hhh4lag class.

## Usage

```

## S3 method for class 'summary.hhh4lag'
print(x, digits = max(3,getOption("digits") - 3), ...)

```

---

profile\_par\_lag

*Estimating the lag decay parameter of an hhh4\_lag model using profile likelihood*

---

## Description

Wrapper around hhh4\_lag to allow for profile likelihood estimation of the scalar parameter governing the lag structure. hhh4\_lag can fit models with fixed lag decay parameter; profile\_par\_lag re-fits the model for different values of par\_lag and finds the optimal value. See ?hhh4\_lag for details. NOTE: fit\_par\_lag serves essentially the same purpose, but is based on a grid of potential values for par\_lag rather than optimization using optim. profile\_par\_lag is the recommended option, but fit\_par\_lag may be somewhat quicker for complex models.

## Usage

```
profile_par_lag(
  sts0bj,
  control,
  start_par_lag = NULL,
  lower_par_lag = -10,
  upper_par_lag = 10,
  return_full_cov = FALSE,
  reltol_par_lag = 1e-08,
  check.analyticals = FALSE
)
```

## Arguments

sts0bj, control, check.analyticals

As in surveillance::hhh4, but control allows for some additional arguments in order to specify a distributed lag structure:

- funct\_lag Function to compute the lag weights  $u_q$  (see details) depending on a scalar parameter par\_lag. The function has to take the following arguments:
  - par\_lag A scalar parameter to steer  $u_q$ . It should be specified in a way which allows it to take any value in the real numbers
  - min\_lag, max\_lag Minimum and maximum lags; e.g. min\_lag = 3, max\_lag = 6 will assign all weights to lags 3 through 6. Usually min\_lag is set to 1, higher values can be useful for direct forecasting at higher horizons.
- min\_lag, max\_lag Specification of the arguments passed to funct\_lag to compute the distributed lags. Unlike in hhh4\_lag, par\_lag is not to be specified as it is estimated from the data. Important: the first element of the subset argument in control needs to be larger than max\_lag (as for the first max\_lag observations the fitted values cannot be computed)

start\_par\_lag A starting value for par\_lag

```

lower_par_lag, upper_par_lag
    lower and upper limits for the value of par_lag; defaults to -10, 10
return_full_cov
    logical: should the full covariance matrix of the parameter estimates (including
    par_lag) be obtained numerically?
reltol_par_lag the relative tolerance passed to the optim call to identify par_lag

```

## Details

The standard hhh4 function only allows for models with first lags i.e. of the form

$$mu_{it} = \lambda_{it} X_{i,t-1} + \phi_{it} \sum_{j \neq i} w_{ji} X_{j,t-1} + \nu_{it},$$

see ?hhh4. The extension hhh4\_lag allows to specify models of the form

$$mu_{it} = \lambda_{it} \sum_{q=1}^Q u_q X_{i,t-q} + \phi_{it} \sum_{j \neq i} \sum_{q=1}^Q w_{ji} u_q X_{j,t-q} + \nu_{it}.$$

Here the first lags are now replaced by weighted sums of the Q previous observations. The weights  $u_q$ ,  $q = 1, \dots, Q$  sum up to 1 and need to be parametrizable by a single scalar parameter. The value of this parameter needs to be passed as control\$par\_lag. Moreover, a function to obtain a vector of weights from par\_lag needs to be provided in control\$funct\_lag. Currently several such functions are implemented in the package:

- Geometric lags (function geometric\_lag; the default). These are specified as

$$u0_q = \alpha * (1 - \alpha)^{q-1}$$

and  $u_q = u0_q / \sum_{q=1}^Q u0_q$  for  $q = 1, \dots, Q$ . The par\_lag parameter corresponds to logit( $\alpha$ ), i.e. the un-normalized weight of the first lag.

- Poisson lags (function poisson\_lag). These are specified as

$$u0_q = \alpha^{(q-1)} \exp(-\alpha) / (q-1)!,$$

and  $u_q = u0_q / \sum_{q=1}^Q u0_q$  for  $q = 1, \dots, Q$ . Note that the Poisson distribution is shifted by one to achieve a positive support. The par\_lag parameter corresponds to log( $\alpha$ ).

- Linearly decaying weights (in function linear\_lag). These are specified as

$$u0_q = \max(1 - mq, 0)$$

and  $u_q = u0_q / \sum_{q=1}^Q u0_q$  for  $q = 1, \dots, Q$ . The par\_lag parameter corresponds to logit( $m$ ).

- A weighting only between first and second lags (in function ar2lag), i.e.

$$u_1 = \alpha, u_2 = 1 - \alpha.$$

The par\_lag parameter corresponds to logit( $\alpha$ ).

- Unrestricted lag can be fitted using unrestricted\_lag. These are parameterized via a multinomial logit transformation where the first lag is the reference category.
- Discretized log-normal lags are implemented in log\_normal\_lag, see details there.

Users can specify their own weighting functions as long as they take the arguments described above and return a vector of weights.

**Value**

If `return_full_cov == FALSE`: an `hhh4_lag` object. If `return_full_cov == TRUE` A list with two elements: `best_mod` is the `hhh4_lag` fit for the best value of `par_lag`; `cov` is an extended covariance matrix for the regression parameters which also includes `par_lag`.

**See Also**

`hhh4_lag` for fitting models with fixed `par_lag`; `fit_par_lag` for grid-based optimization.

**Examples**

```
## a simple univariate example:
data("salmonella.agona")
## convert old "disProg" to new "sts" data class
salmonella <- disProg2sts(salmonella.agona)
# specify and fit model: fixed geometric lag structure
control_salmonella <- list(end = list(f = addSeason2formula(~ 1)),
                           ar = list(f = addSeason2formula(~ 1)),
                           family = "NegBinM", subset = 6:312)
fit_salmonella <- profile_par_lag(salmonella, control_salmonella)
summary(fit_salmonella)
# 0.56 on first lag
#
# re-fit with Poisson lags:
control_salmonella2 <- control_salmonella
control_salmonella2$funct_lag = poisson_lag
fit_salmonella2 <- profile_par_lag(salmonella, control_salmonella2)
summary(fit_salmonella2)
# leads to somewhat different decay and very slightly better AIC
```

`psi2size.hhh4lag`      *A modified version of psi2size.hhh4*

**Description**

A modified version of `psi2size.hhh4` to deal with the added features of the `hhh4lag` class. Extracts estimated overdispersion in `dnbnom()` parametrization (and as matrix)

**Usage**

```
psi2size.hhh4lag(object, subset = object$control$subset, units = NULL)
```

---

quantile.oneStepAhead *quantiles of the one-step-ahead forecasts*

---

### Description

quantiles of the one-step-ahead forecasts

### Usage

```
## S3 method for class 'oneStepAhead'  
quantile(x, probs = c(2.5, 10, 50, 90, 97.5)/100, ...)
```

---

ranef.hhh4lag *A modified version of ranef.hhh4*

---

### Description

A modified version of ranef.hhh4

### Usage

```
## S3 method for class 'hhh4lag'  
ranef(object, tomatrix = FALSE, intercept = FALSE, ...)
```

---

residuals.hhh4lag *A modified version of residuals.hhh4*

---

### Description

A modified version of residuals.hhh4 to deal with the added features of the hhh4lag class. Computes deviance residuals.

### Usage

```
## S3 method for class 'hhh4lag'  
residuals(object, type = c("deviance", "response"), ...)
```

simulate.hhh4lag	<i>Simulate "hhh4_lag" Count Time Series</i>
------------------	----------------------------------------------

### Description

This function is the equivalent of `surveillance::simulate.hhh4` for model fits of class `hhh4lag`, obtained from `hhh4_lag` or `profile_par_lag`. The arguments are the same as in `surveillance::simulate.hhh4`, the only difference being that `y.start` needs to be a matrix with `object$control$max_lag` rows and `object$nUnit` columns.

### Usage

```
## S3 method for class 'hhh4lag'
simulate(
  object,
  nsim = 1,
  seed = NULL,
  y.start = NULL,
  subset = 1:nrow(object$stsObj),
  coefs = coef(object),
  components = c("ar", "ne", "end"),
  simplify = nsim > 1,
  ...
)
```

### Details

This function is still being tested!!!

stationary_moments	<i>Analytic calculation of periodically stationary moments implied by a hhh4-model</i>
--------------------	----------------------------------------------------------------------------------------

### Description

Returns the mean vector and covariance matrix of the periodically stationary distribution implied by an `hhh4` object.

### Usage

```
stationary_moments(
  hhh4Obj,
  start = 1,
  n_seasons = 1,
  return_Sigma = FALSE,
```

```

    return_cov_array = FALSE,
    return_mu_decomposed = FALSE,
    return_M = FALSE,
    max_iter = 10,
    tolerance = 1e-05
)

```

### Arguments

hhh4obj	hhh4 object for which to calculate stationary moments
start	start of the season
n_seasons	number of
return_Sigma	logical: return entire variance/covariance matrix of the prediction; can take a lot of storage
return_cov_array	logical: return an array containing week-wise covariance matrices
return_mu_decomposed	logical: return an array containing a decomposition of stationary means into the three components endemic, epi.own and epi.others.
return_M	logical: return the array M containing un-centered second moments (used internally for calculations)
max_iter	maximum number of iterations before iterative algorithm stops
tolerance	element-wise maximum tolerance (entering into termination criterion for the iterative calculation)

### Value

An object of class `stationary_moments_hhh4` containing the following components:

- `mu_matrix` A matrix containing the stationary means. Each row corresponds to a time period and each column to a unit.
- `var_matrix` A matrix containing the stationary variances.
- `cov_array` An array containing time period-wise variance-covariance matrices.
- `mu_vector` as `mu_matrix`, but flattened into a vector.
- `Sigma` a large covariance matrix for all elements of the prediction (corresponding to `mu_vector`)
- `M` a matrix containing stationary means and (un-centered) second moments, specifically  $E(c(1, X))$  Important in the internal calculation, accessible mainly for de-bugging purposes.
- `mu_decomposed` an array with the same number of rows and columns as `mu_matrix`, but three layers corresponding to the contributions of the three components to the means
- `start` the position (within a cycle) of the time period to which the first elements of `mu_matrix` etc. correspond (i.e. the `start` argument from the call of `stationary_moments`)
- `freq` the length of a cycle
- `n_seasons` the number of seasons covered in `mu_matrix` etc.
- `n_units` the number of units covered in the prediction

- timepoints the positions within a cycle of the timepoints covered by mu\_matrix etc.
- condition NULL. Only relevant in predictive moments, just a place holder here.
- type "stationary"; to distinguish from predictive moments.
- has\_temporal\_structure does the object still have the original temporal structure? can be set to FALSE when aggregated using aggregate\_prediction.

## Examples

```

data("salmonella.agona")
## convert old "disProg" to new "sts" data class
salmonella <- disProg2sts(salmonella.agona)
# specify and fit model
control_salmonella <- list(end = list(f = addSeason2formula(~ 1), lag = 1),
                           ar = list(f = addSeason2formula(~ 1), lag = 1),
                           family = "NegBinM")
fit_salmonella <- hhh4(salmonella, control_salmonella)
# obtain periodically stationary moments:
stat_mom <- stationary_moments(fit_salmonella)
# plot periodically stationary means:
fanplot_stationary(stat_mom)
# add paths of the six seasons in the data set:
for(i in 0:5){
  lines(1:52/52, salmonella@observed[(i*52 + 1):((i + 1)*52)], col = "blue")
}
legend("topleft", col = "blue", lty = 1, legend = "observed seasons")

```

summary.hhh4lag

*A modified version of surveillance::summary.hhh4*

## Description

A modified version of surveillance::summary.hhh4 to deal with the added features of the hhh4lag class.

## Usage

```

## S3 method for class 'hhh4lag'
summary(object, maxEV = FALSE, ...)

```

---

terms.hhh4lag	<i>A modified version of terms.hhh4</i>
---------------	-----------------------------------------

---

## Description

A modified version of `terms.hhh4` to deal with the added features of the `hhh4lag` class.

## Usage

```
## S3 method for class 'hhh4lag'  
terms(x, ...)
```

---

unrestricted_lag	<i>Function to obtain unrestricted lags</i>
------------------	---------------------------------------------

---

## Description

This function generates  $Q$  lag weights without a parametric constraint. The weights are obtained via a multinomial logit transformation where the first lag is the reference category.

## Usage

```
unrestricted_lag(par_lag, min_lag, max_lag)
```

## Arguments

- |                      |                                                                                                               |
|----------------------|---------------------------------------------------------------------------------------------------------------|
| <code>par_lag</code> | the parameter vector of length $Q - 1$                                                                        |
| <code>min_lag</code> | smallest lag to include; the support of the Poisson form starts only at <code>min_lag</code> . Defaults to 1. |
| <code>max_lag</code> | highest lag to include; higher lags are cut off and the remaining weights standardized. Defaults to 5.        |

---

`update.hhh4lag`*A modified version of update.hhh4*

---

## Description

A modified version of `update.hhh4` to deal with the added features of the `hhh4lag` class. Note that the lag weights are not re-estimated!

## Usage

```
## S3 method for class 'hhh4lag'  
update(  
  object,  
  refit_par_lag = TRUE,  
  ...,  
  S = NULL,  
  subset.upper = NULL,  
  use.estimates = object$convergence,  
  evaluate = TRUE,  
  warning_weights = TRUE  
)
```

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